



basic education

Department:
Basic Education
REPUBLIC OF SOUTH AFRICA

**NATIONAL
SENIOR CERTIFICATE
*NASIONALE SENIOR
SERTIFIKAAT***

GRADE 12/*GRAAD 12*

MATHEMATICS P2/*WISKUNDE V2*

NOVEMBER 2017

MARKING GUIDELINES/*NASIENRIGLYNE*

MARKS/*PUNTE*: 150

**These marking guidelines consist of 29 pages.
*Hierdie nasienriglyne bestaan uit 28 bladsye.***

NOTE:

- If a candidate answers a question TWICE, only mark the FIRST attempt.
- If a candidate has crossed out an attempt of a question and not redone the question, mark the crossed out version.
- Consistent accuracy applies in ALL aspects of the marking guidelines. Stop marking at the second calculation error.
- Assuming answers/values in order to solve a problem is NOT acceptable.

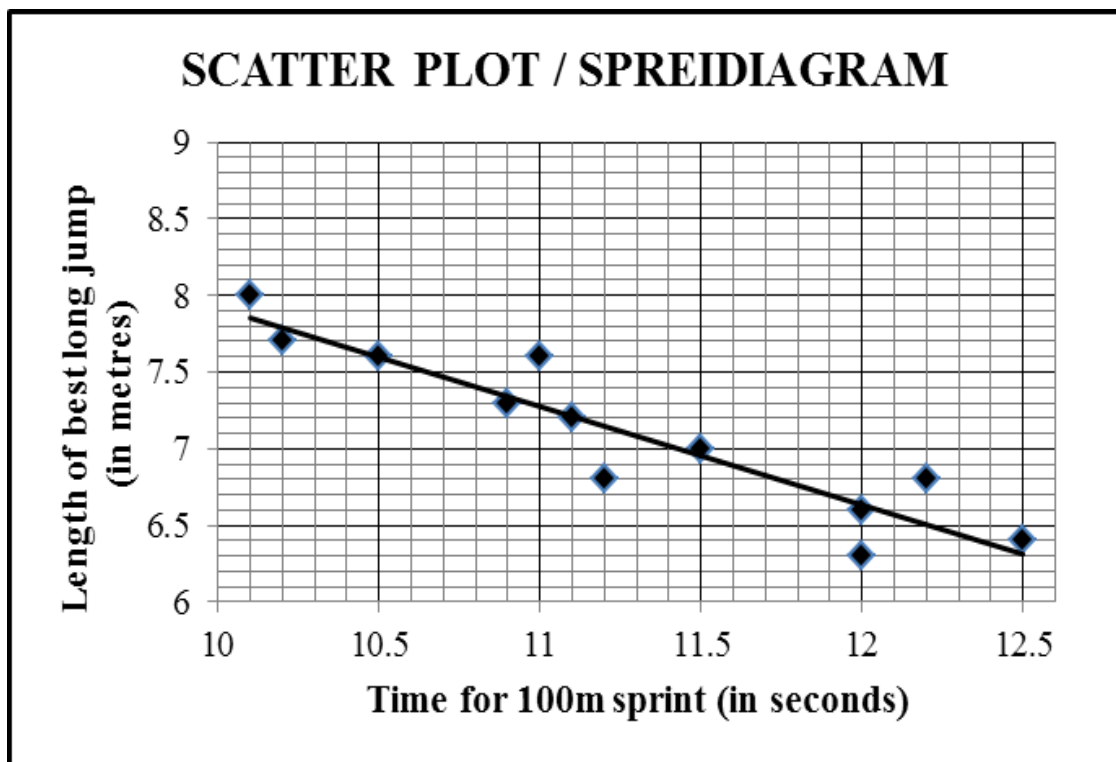
NOTA:

- *As 'n kandidaat 'n vraag TWEE KEER beantwoord, merk slegs die EERSTE poging.*
- *As 'n kandidaat 'n antwoord van 'n vraag doodtrek en nie oordoen nie, merk die doodgetrekte poging.*
- *Volgehoue akkuraatheid word in ALLE aspekte van die nasienriglyne toegepas. Hou op nasien by die tweede berekeningsfout.*
- *Aanvaar van antwoorde/waardes om 'n probleem op te los, word NIE toegelaat nie.*

| GEOMETRY | |
|-----------------|--|
| S | A mark for a correct statement (A statement mark is independent of a reason.) |
| | 'n Punt vir 'n korrekte bewering ('n Punt vir 'n bewering is onafhanklik van die rede.) |
| R | A mark for a correct reason (A reason mark may only be awarded if the statement is correct.) |
| | 'n Punt vir 'n korrekte rede ('n Punt word slegs vir die rede toegeken as die bewering korrek is.) |
| S/R | Award a mark if the statement AND reason are both correct. |
| | Ken 'n punt toe as beide die bewering EN rede korrek is. |

QUESTION/VRAAG 1

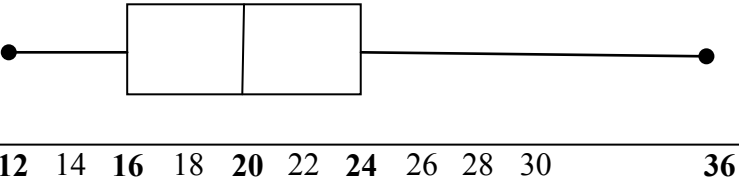
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|--|------|------|------|------|-----|------|------|------|-----|-----|------|------|
| Time for 100 m sprint (in seconds) <i>Tyd vir 100 m-naelloop (in sekondes)</i> | 10,1 | 10,2 | 10,5 | 10,9 | 11 | 11,1 | 11,2 | 11,5 | 12 | 12 | 12,2 | 12,5 |
| Distance of best long jump (in metres) <i>Afstand van beste sprong in verspring (in meter)</i> | 8 | 7,7 | 7,6 | 7,3 | 7,6 | 7,2 | 6,8 | 7 | 6,6 | 6,3 | 6,8 | 6,4 |



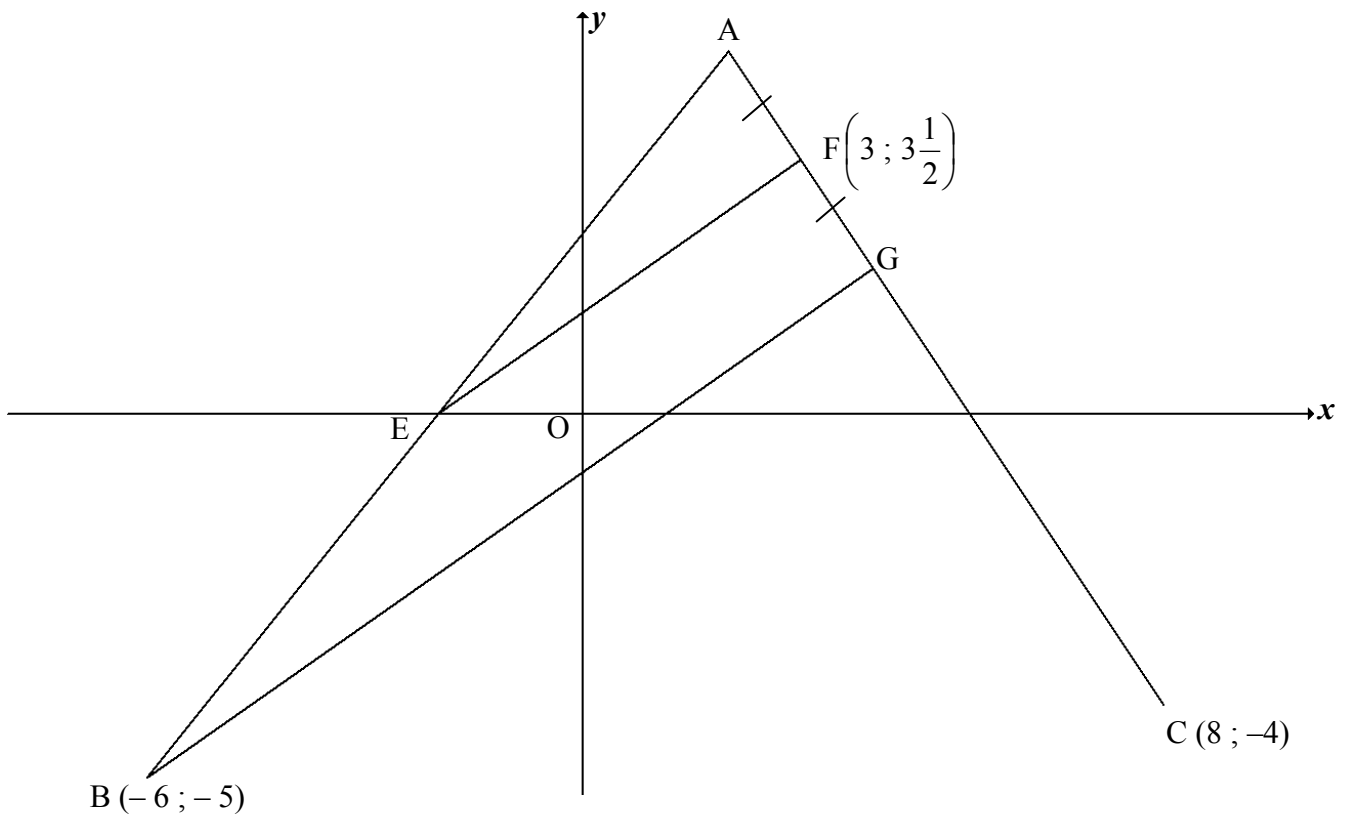
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| 1.1 | $a = 14,343\dots = 14,34$ $b = -0,642\dots = -0,64$ | ✓✓ value of a ✓ value of b (3) |
| 1.2 | $y = 14,34 - 0,64(11,7)$ $= 6,85$ OR/OF $y = 6,83$ (calculator / <i>sakrekenaar</i>) | ✓ substitution correctly ✓ answer ✓✓ answer (2) (2) |
| 1.3 | The gradient increases / <i>Die gradient neem toe</i> The point (12,3 ; 7,6) lies some distance above the current data. <i>/Die punt (12,3 ; 7,6) lê bokant die huidige data.</i> | ✓ increases/ <i>neem toe</i> ✓ reasoning in words/ <i>redenasie in woorde</i> (2) [7] |

QUESTION/VRAAG 2

| | | | | | | | | | | | |
|----|----|----|----|----|----|----|----|----|----|----|----|
| 12 | 13 | 13 | 14 | 14 | 16 | 17 | 18 | 18 | 18 | 19 | 20 |
| 21 | 21 | 22 | 22 | 23 | 24 | 25 | 27 | 29 | 30 | 36 | |

| | | |
|-------|--|--|
| 2.1.1 | $\bar{x} = \frac{472}{23}$ $\bar{x} = 20,52 \text{ seconds / sekonde}$ | ✓ $\frac{472}{23}$ ✓ answer (2) |
| 2.1.2 | $Q_1 = 16$ $Q_3 = 24$ $IQR/IKO = Q_3 - Q_1$ $= 24 - 16 = 8$ | ✓ Q_1 ✓ Q_3 ✓ answer (3) |
| 2.2 | $20,52 + 5,94 = 26,46$ $\therefore > 26,46$ $\therefore 4 \text{ girls/dogters}$ | ✓ 26,46 ✓ answer (2) |
| 2.3 |  <p>12 14 16 18 20 22 24 26 28 30 36</p> | ✓ whiskers ending at 12 & 36 ✓ $Q_1 = 16$ & $Q_3 = 24$ (box) ✓ $Q_2 = 20$ (3) |
| 2.4.1 | Girls / Meisies | ✓ answer (1) |
| 2.4.2 | Five-number summary of boys: (15 ; 21 ; 23,5 ; 26 ; 38) None of the boys / Nie een van die seuns nie 5 girls completed in less than 15 seconds which was the minimum time taken by the boys. 5 meisies voltooi in minder as 15 sekondes, wat die minimumtyd is wat die seuns geneem het. | ✓ answer ✓ reason/rede (2) [13] |

QUESTION/VRAAG 3



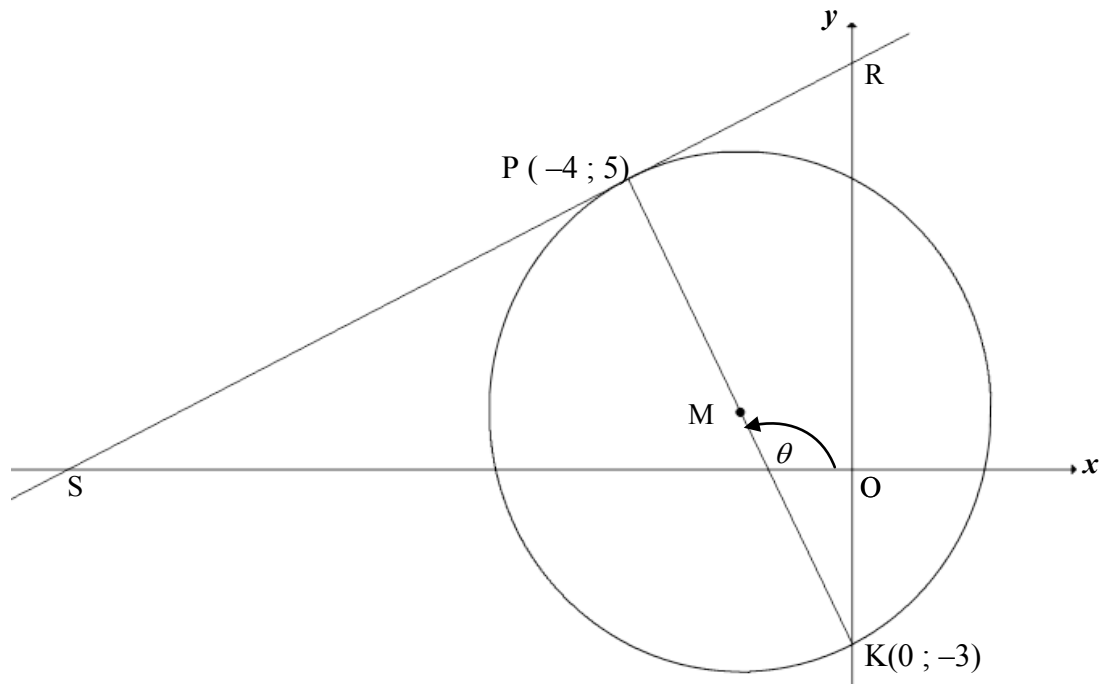
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| <p>3.1.1</p> | $m_{FC} = \frac{y_2 - y_1}{x_2 - x_1}$ $= \frac{3\frac{1}{2} - (-4)}{3 - 8}$ $= -\frac{3}{2}$ <p>$y = mx + c$ $y - y_1 = m(x - x_1)$</p> $y = -\frac{3}{2}x + c$ $-4 = -\frac{3}{2}(8) + c \quad \text{OR/OF} \quad (y - (-4)) = -\frac{3}{2}(x - 8)$ $c = 8$ $y = -\frac{3}{2}x + 8$ <p>OR/OF</p> $y + 4 = -\frac{3}{2}x + 12$ $y = -\frac{3}{2}x + 8$ | <ul style="list-style-type: none"> ✓ substitution of (8 ; -4) & $(3; 3\frac{1}{2})$ ✓ gradient ✓ substitution of m and (8 ; -4) ✓ equation of AC <p style="text-align: right;">(4)</p> |
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| | $m_{FC} = \frac{y_2 - y_1}{x_2 - x_1} = \frac{(-4) - \left(3\frac{1}{2}\right)}{8 - 3}$ $= -\frac{3}{2}$ $y = mx + c$ $3\frac{1}{2} = -\frac{3}{2}(3) + c$ $c = 8$ $y = -\frac{3}{2}x + 8$ $y - y_1 = m(x - x_1)$ $\left(y - 3\frac{1}{2}\right) = -\frac{3}{2}(x - 3)$ <p style="text-align: center;">OR/OF</p> $\left(y - 3\frac{1}{2}\right) = -\frac{3}{2}x + \frac{9}{2}$ $y = -\frac{3}{2}x + 8$ | <ul style="list-style-type: none"> ✓ substitution of $(8 ; -4)$ & $\left(3 ; 3\frac{1}{2}\right)$ ✓ gradient ✓ substitution of m and $\left(3 ; 3\frac{1}{2}\right)$ ✓ equation of AC <p style="text-align: right;">(4)</p> |
| <p>3.1.2</p> | <p>AC: $3x + 2y = 16$ and BG: $7x - 10y = 8$</p> $15x + 10y = 80$ $\underline{7x - 10y = 8}$ $22x = 88$ $x = 4$ $3(4) + 2y = 16$ $y = 2$ <p>∴ G(4 ; 2)</p> <p>OR/OF</p> <p>BG: $7x - 10y = 8$ ∴ $y = \frac{7}{10}x - \frac{8}{10}$</p> $\therefore \frac{7}{10}x - \frac{8}{10} = -\frac{3}{2}x + 8 \quad [\text{CA from 3.1.1}]$ $\frac{11}{5}x = \frac{44}{5}$ $x = 4$ $3(4) + 2y = 16$ $y = 2$ <p>∴ G(4 ; 2)</p> | <ul style="list-style-type: none"> ✓ method /metode: solving simultaneously / los gelyktydig op ✓ x coordinate ($x > 0$) ✓ y coordinate <p style="text-align: right;">(3)</p> <ul style="list-style-type: none"> ✓ method: equating metode: stel vgl's gelyk ✓ x coordinate ($x > 0$) ✓ y coordinate <p style="text-align: right;">(3)</p> |
| <p>3.2</p> | $\frac{x_A + 4}{2} = 3 \quad \text{and} \quad \frac{y_A + 2}{2} = 3\frac{1}{2}$ <p>∴ A(2 ; 5)</p> <p>OR/OF by translation/deur translasië:</p> $x_A = 3 - (4 - 3) = 2$ $y_A = 3\frac{1}{2} + (3\frac{1}{2} - 2) = 5$ <p>∴ A(2 ; 5)</p> | <ul style="list-style-type: none"> ✓ equation ito x ✓ equation ito y <p style="text-align: right;">(2)</p> <ul style="list-style-type: none"> ✓ equation ito x ✓ equation ito y <p style="text-align: right;">(2)</p> |

| | | |
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| <p>3.3</p> | <p>The coordinates of the midpt of AB / <i>Die koordinaat van midpt van AB is:</i></p> $\left(\frac{2+(-6)}{2}; \frac{5+(-5)}{2}\right) = (-2; 0)$ <p>But the y-coordinate of E is 0 ∴ E(-2 ; 0) is the midpoint of AB ∴ EF BG [midpoint theorem/<i>middelpuntst</i> OR/OF line divides 2 sides of Δ in prop/lyn <i>verdeel 2 sye van Δ in dies verh</i>]</p> <p>OR/OF The coordinates of the midpt of AB / <i>Die koordinaat van midpt van AB is:</i></p> $\left(\frac{2+(-6)}{2}; \frac{5+(-5)}{2}\right) = (-2; 0)$ $AE = \sqrt{(-2-2)^2 + (0-5)^2} = \sqrt{41}$ $EB = \sqrt{(-2-(-6))^2 + (0-(-5))^2} = \sqrt{41}$ <p>∴ In ΔABG: AE = EB and AF = FG ∴ EF BG [midpoint theorem/<i>middelpuntst</i>]</p> <p>OR/OF Equation of AB:</p> $y - (-5) = \left(\frac{5-(-5)}{2-(-6)}\right)(x - (-6))$ $y + 5 = \frac{10}{8}x + \frac{15}{2} \quad \therefore y = \frac{5}{4}x + \frac{5}{2}$ <p>x-intercept of AB:</p> $0 = \frac{5}{4}x + \frac{5}{2} \quad \therefore x = -2$ <p>∴ E(-2 ; 0)</p> $m_{EF} = \frac{3\frac{1}{2} - 0}{3 - (-2)} = \frac{7}{10}$ $m_{EF} = m_{BG} = \frac{7}{10}$ <p>∴ EF BG</p> <div style="border: 1px solid black; padding: 5px; width: fit-content; margin: 10px auto;"> <p>BG: $7x - 10y = 8$ $\therefore y = \frac{7}{10}x - \frac{8}{10}$ $\therefore m_{BG} = \frac{7}{10}$</p> </div> | <p>✓ subst A & B into midpt formula ✓ y coordinate = 0</p> <p>✓ E = midpt ✓ Reason (4)</p> <p>✓ subst A & B into midpt formula ✓ lengths of AE & EB</p> <p>✓ AE = EB or E = midpt ✓ Reason (4)</p> <p>✓ equation of AB</p> <p>✓ coordinates of E</p> <p>✓ gradient of EF ✓ gradient EF = gradient BG (4)</p> |
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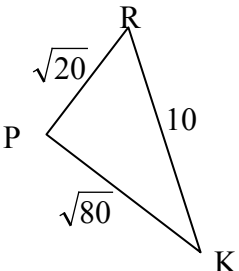
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| 3.4 | <p>Midpoint of AC = $\left(5; \frac{1}{2}\right)$</p> $\frac{x_D + (-6)}{2} = 5 \quad \text{and} \quad \frac{y_D + (-5)}{2} = \frac{1}{2}$ <p>$\therefore D(16; 6)$</p> <p>OR/OF by translation/<i>dmv translasië</i>: D(16; 6)</p> <p>OR/OF</p> $m_{BC} = \frac{-5 - (-4)}{-6 - 8} = \frac{1}{14} \quad \text{and} \quad m_{AB} = \frac{5 - (-5)}{2 - (-6)} = \frac{5}{4}$ <p>AD: $y - 5 = \frac{1}{14}(x - 2) \Rightarrow y = \frac{1}{14}x + \frac{34}{7}$</p> <p>CD: $y + 4 = \frac{5}{4}(x - 8) \Rightarrow y = \frac{5}{4}x - 14$</p> $\frac{5}{4}x - 14 = \frac{1}{14}x + \frac{34}{7}$ <p>$\therefore \quad x = 16$ $\quad \quad y = 6$</p> | <p>$\checkmark\checkmark \left(5; \frac{1}{2}\right)$</p> <p>$\checkmark$ x value \checkmark y value (4)</p> <p>\checkmark method finding x \checkmark method finding y \checkmark x value \checkmark y value (4)</p> <p>$\checkmark\checkmark$ equating \checkmark x value \checkmark y value (4)</p> <p>[17]</p> |
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QUESTION/VRAAG 4



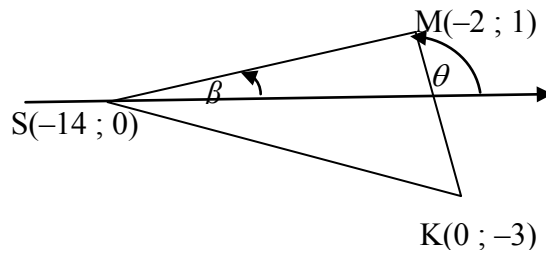
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| <p>4.1.1</p> | $m_{PK} = \frac{5 - (-3)}{-4 - 0}$ $= -2$ <p>$PK \perp SR$ [radius \perp tangent/raaklyn]</p> $\therefore m_{PK} \times m_{RS} = -1$ $\therefore m_{RS} = \frac{1}{2}$ | <ul style="list-style-type: none"> ✓ substitution P & K into gradient formula ✓ gradient of PK ✓ $PK \perp SR$ OR $r \perp$ tangent ✓ answer <p style="text-align: right;">(4)</p> |
| <p>4.1.2</p> | $y = \frac{1}{2}x + c$ $5 = \frac{1}{2}(-4) + c \quad \mathbf{OR/OR} \quad (y - 5) = \frac{1}{2}(x - (-4))$ $c = 7 \quad (y - 5) = \frac{1}{2}x + 2$ $y = \frac{1}{2}x + 7 \quad y = \frac{1}{2}x + 7$ | <ul style="list-style-type: none"> ✓ substitution of m and P ✓ equation <p style="text-align: right;">(2)</p> |

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| <p>4.1.3</p> | $M\left(\frac{-4+0}{2}; \frac{5+(-3)}{2}\right)$ $\therefore M(-2; 1)$ $r^2 = (x_2 - x_1)^2 + (y_2 - y_1)^2$ $r^2 = (-2 + 4)^2 + (1 - 5)^2$ $\therefore r^2 = 20$ $\therefore (x + 2)^2 + (y - 1)^2 = 20 \text{ or } (\sqrt{20})^2$ <p>OR/OF</p> $M\left(\frac{-4+0}{2}; \frac{5+(-3)}{2}\right) \therefore M(-2; 1)$ $(x + 2)^2 + (y - 1)^2 = r^2$ $(-4 + 2)^2 + (5 - 1)^2 = r^2$ $\therefore r^2 = 20$ $\therefore (x + 2)^2 + (y - 1)^2 = 20 \text{ or } (\sqrt{20})^2$ <p>OR/OF</p> $M\left(\frac{-4+0}{2}; \frac{5+(-3)}{2}\right) \therefore M(-2; 1)$ $PK = \sqrt{(-4 - 0)^2 + (5 - (-3))^2} = \sqrt{80}$ $r = \frac{\sqrt{80}}{2} = \sqrt{20}$ $\therefore (x + 2)^2 + (y - 1)^2 = 20 \text{ or } (\sqrt{20})^2$ | <p>✓ x value of M ✓ y value of M</p> <p>✓ $r^2 = 20$</p> <p>✓ equation (4)</p> <p>✓✓ M (- 2 ; 1)</p> <p>$r^2 = 20$</p> <p>✓ equation (4)</p> <p>✓✓ M (- 2 ; 1)</p> <p>$r^2 = 20$</p> <p>✓ equation (4)</p> |
|--------------|--|--|

| | | |
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| <p>4.1.4</p> | <p> $\tan \theta = m_{PK} = -2$ $\therefore \theta = 180^\circ - 63,43^\circ$ $= 116,57^\circ$ $\hat{P}KR = 116,57^\circ - 90^\circ$ [ext \angle of ΔMOK] $= 26,57^\circ$ OR/OF </p>  <p> <u>In ΔRPK:</u> $PK = \sqrt{(0 - (-4))^2 + (-3 - 5)^2} = \sqrt{80}$ $PR = \sqrt{(-4 - 0)^2 + (5 - 7)^2} = \sqrt{20}$ $RK = 10$ $\cos \hat{P}KR = \frac{PK^2 + KR^2 - PR^2}{2 \cdot PK \cdot KR} = \frac{(\sqrt{80})^2 + (10)^2 - (\sqrt{20})^2}{2(\sqrt{80})(10)}$ $= \frac{2\sqrt{5}}{5}$ $\hat{P}KR = 26,57^\circ$ OR/OF </p> <p> $\sin \hat{P}KR = \frac{\sqrt{20}}{10}$ OR/OF $\cos \hat{P}KR = \frac{\sqrt{80}}{10}$ $\hat{P}KR = 26,57^\circ$ $\hat{P}KR = 26,57^\circ$ OR/OF </p> <p> $\tan \hat{P}KR = \frac{\sqrt{20}}{\sqrt{80}}$ $\hat{P}KR = 26,57^\circ$ </p> | <p> $\checkmark \tan \theta = -2$ \checkmark size of θ \checkmark answer (3) </p> <p> \checkmark lengths of PK, PR & RK \checkmark correct values into cos rule \checkmark answer (3) </p> <p> \checkmark lengths of sides \checkmark ratio \checkmark answer (3) </p> <p> \checkmark lengths of sides \checkmark ratio \checkmark answer (3) </p> |
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| 4.1.5 | <p>RS tangent at K(0 ; -3)</p> $\therefore m_{PS} = m_{\text{tang}} = \frac{1}{2}$ $\therefore y = \frac{1}{2}x - 3$ <p>OR/OF</p> $m_{PK} = \frac{1-5}{-2+4} = -2$ $m_{PK} \times m_{\text{tang}} = -1 \quad [\text{radius } \perp \text{ tangent/raaklyn}]$ $\therefore m_{\text{tang}} = \frac{1}{2}$ $\therefore y = \frac{1}{2}x - 3$ | <p>✓ gradient</p> <p>✓ equation (2)</p> <p>✓ gradient</p> <p>✓ equation (2)</p> |
| 4.2 | <p>$t \in (-3 ; 7)$</p> <p>OR/OF</p> $-3 < t < 7$ | <p>✓ -3 (A)</p> <p>✓ 7 (CA from 4.1.2)</p> <p>✓ correct inequality (3)</p> <p>✓ -3 (A)</p> <p>✓ 7 (CA from 4.1.2)</p> <p>✓ correct inequality (3)</p> |
| 4.3 | <p>RS: $y = \frac{1}{2}x + 7 \quad \therefore S(-14 ; 0)$</p> $SP = \sqrt{(-14 - (-4))^2 + (0 - 5)^2} = \sqrt{100 + 25} = \sqrt{125}$ $\text{Area } \triangle SMK = \frac{1}{2} \cdot MK \cdot SP$ $= \frac{1}{2} (\sqrt{20})(\sqrt{125})$ $= 25 \text{ square units}$ | <p>✓ coordinates of S</p> <p>✓ length of SP</p> <p>✓ correct base & height into Area rule</p> <p>✓ correct substitution</p> <p>✓ answer (5)</p> |

OR/OF



Let β = inclination of SM/ *inklinasie van SM*

RS: $y = \frac{1}{2}x + 7 \quad \therefore S(-14; 0)$

$$SM = \sqrt{(-14 - (-2))^2 + (0 - 1)^2} = \sqrt{145}$$

$$\tan \beta = \frac{1 - 0}{-2 - (-14)} = \frac{1}{12} \quad \therefore \beta = 4,76^\circ$$

$$\therefore \hat{SMK} = 116,57^\circ - 4,76^\circ \quad [\text{ext } \angle \text{ of } \Delta]$$

$$= 111,81^\circ$$

$$\text{Area } \Delta SMK = \frac{1}{2}(SM)(MK) \cdot \sin \hat{SMK}$$

$$= \frac{1}{2}(\sqrt{145})(\sqrt{20}) \cdot \sin 111,81^\circ$$

$$= 24,9985 = 25 \text{ square units}$$

✓ coordinates of S

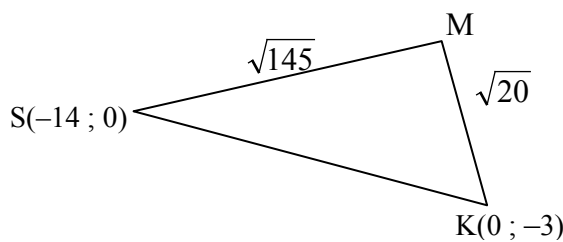
✓ length of SM

✓ size of/grootte v \hat{SMK}

✓ correct substitution into area rule
 ✓ answer

(5)

OR/OF



RS: $y = \frac{1}{2}x + 7 \quad \therefore S(-14; 0)$

$$SK = \sqrt{(-14 - 0)^2 + (0 + 3)^2} = \sqrt{205}$$

$$\cos \hat{SMK} = \frac{(\sqrt{145})^2 + (\sqrt{20})^2 - (\sqrt{205})^2}{2(\sqrt{145})(\sqrt{20})} = -\frac{2\sqrt{29}}{29}$$

$$\hat{SMK} = 111,80^\circ$$

$$\text{Area } \Delta SMK = \frac{1}{2}(SM)(MK) \cdot \sin \hat{SMK}$$

$$= \frac{1}{2}(\sqrt{145})(\sqrt{20}) \cdot \sin 111,81^\circ$$

$$= 24,9985 = 25 \text{ square units}$$

✓ coordinates of S

✓ length of SK

✓ size of/grootte v \hat{SMK}

✓ correct substitution into area rule
 ✓ answer

(5)

| | | |
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| | <p>OR/OF</p> <p>Produce KS to T</p> <p>RS: $y = \frac{1}{2}x + 7 \quad \therefore S(-14; 0)$</p> <p>$SK = \sqrt{(-14 - 0)^2 + (0 + 3)^2} = \sqrt{205}$</p> <p>$SM = \sqrt{(-14 - (-2))^2 + (0 - 1)^2} = \sqrt{145}$</p> <p>$m_{SK} = -\frac{3}{14} \Rightarrow T\hat{S}O = 167,91^\circ$</p> <p>$m_{SM} = \frac{1}{12} \Rightarrow M\hat{S}O = 4,76^\circ$</p> <p>$M\hat{S}K = 180^\circ - 167,91^\circ + 4,76^\circ = 16,85^\circ$</p> <p>Area $\Delta SMK = \frac{1}{2}(SM)(SK) \cdot \sin M\hat{S}K$</p> <p>$= \frac{1}{2}(\sqrt{145})(\sqrt{205}) \cdot \sin 16,85^\circ$</p> <p>$= 24,9985 = 25 \text{ square units}$</p> | <p>✓ coordinates of S</p> <p>✓ length of SK & SM</p> <p>✓ size of /grootte v $M\hat{S}K$</p> <p>✓ correct substitution into area rule</p> <p>✓ answer</p> <p>(5)</p> |
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QUESTION/VRAAG 5

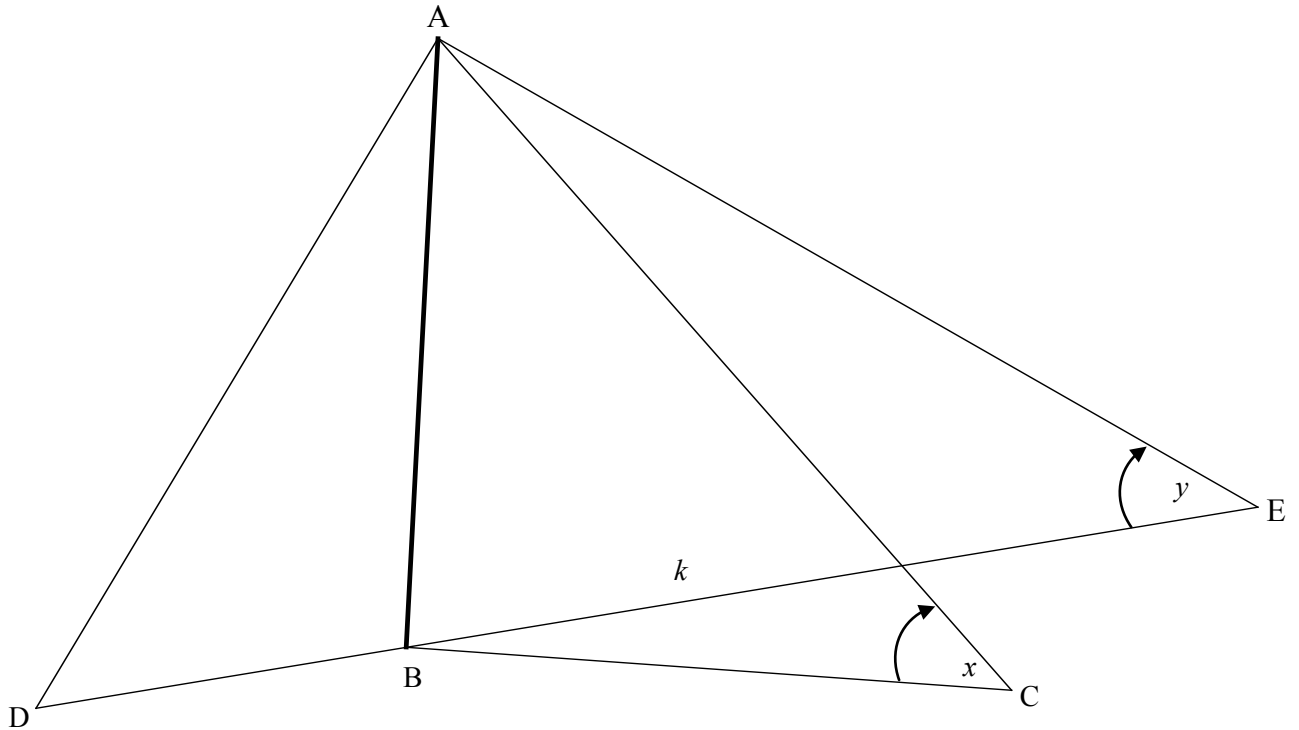
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| 5.1 | $\frac{\sin(A - 360^\circ) \cdot \cos(90^\circ + A)}{\cos(90^\circ - A) \cdot \tan(-A)}$ $= \frac{\sin A(-\sin A)}{\sin A(-\tan A)}$ $= \frac{\sin A}{\left(\frac{\sin A}{\cos A}\right)}$ $= \cos A$ | <ul style="list-style-type: none"> ✓ sin A ✓ -sin A ✓ sin A ✓ -tan A ✓ $\tan A = \frac{\sin A}{\cos A}$ ✓ answer | (6) |
| 5.2.1 | $t^2 = (\sqrt{34})^2 - (3)^2$ $\therefore t = -5$ | <ul style="list-style-type: none"> ✓ substitution ✓ answer | (2) |
| 5.2.2 | $\tan \beta = \frac{-5}{3}$ | <ul style="list-style-type: none"> ✓ correct ratio | (1) |
| 5.2.3 | $\cos 2\beta = 2 \cos^2 \beta - 1$ $= 2 \left(\frac{3}{\sqrt{34}} \right)^2 - 1$ $= 2 \left(\frac{9}{34} \right) - 1$ $= -\frac{16}{34} \text{ OR } -\frac{8}{17}$ <p>OR/OF</p> $\cos 2\beta = 1 - 2 \sin^2 \beta$ $= 1 - 2 \left(-\frac{5}{\sqrt{34}} \right)^2$ $= 1 - 2 \left(\frac{25}{34} \right)$ $= -\frac{16}{34} \text{ OR } -\frac{8}{17}$ <p>OR/OF</p> $\cos 2\beta = \cos^2 \beta - \sin^2 \beta$ $= \left(\frac{3}{\sqrt{34}} \right)^2 - \left(-\frac{5}{\sqrt{34}} \right)^2$ $= \frac{9}{34} - \frac{25}{34}$ $= -\frac{16}{34} \text{ OR } -\frac{8}{17}$ | <ul style="list-style-type: none"> ✓ compound formula ✓ substitution ✓ simplification ✓ answer | (4) |
| | | <ul style="list-style-type: none"> ✓ compound formula ✓ substitution ✓ simplification ✓ answer | (4) |
| | | <ul style="list-style-type: none"> ✓ compound formula ✓ substitution ✓ simplification ✓ answer | (4) |

| | | |
|--------------|--|---|
| <p>5.3.1</p> | <p>LHS = $\sin(A + B) - \sin(A - B)$ $= \sin A \cdot \cos B + \cos A \cdot \sin B - (\sin A \cdot \cos B - \cos A \cdot \sin B)$ $= \sin A \cdot \cos B + \cos A \cdot \sin B - \sin A \cdot \cos B + \cos A \cdot \sin B$ $= 2\cos A \cdot \sin B$ $= \text{RHS}$</p> | <p>✓ compound formula ✓ compound formula (2)</p> |
| <p>5.3.2</p> | <p>$\sin 77^\circ - \sin 43^\circ = \sin(60^\circ + 17^\circ) - \sin(60^\circ - 17^\circ)$ $= 2\cos 60^\circ \cdot \sin 17^\circ$ $= 2 \times \frac{1}{2} \times \sin 17^\circ$ $= \sin 17^\circ$</p> <p>OR/OF</p> <p>$\sin 77^\circ - \sin 43^\circ = \sin(60^\circ + 17^\circ) - \sin(60^\circ - 17^\circ)$ $= (\sin 60^\circ \cos 17^\circ + \cos 60^\circ \sin 17^\circ) -$ $(\sin 60^\circ \cos 17^\circ - \cos 60^\circ \sin 17^\circ)$ $= \frac{\sqrt{3}}{2} \cos 17^\circ + \frac{1}{2} \sin 17^\circ - \frac{\sqrt{3}}{2} \cos 17^\circ + \frac{1}{2} \sin 17^\circ$ $= \sin 17^\circ$</p> | <p>✓ $60^\circ + 17^\circ$ ✓ $60^\circ - 17^\circ$ ✓ simplify ✓ $\frac{1}{2}$ (4)</p> <p>✓ $60^\circ + 17^\circ$ ✓ $60^\circ - 17^\circ$ ✓ expansion ✓ $\frac{1}{2}$ (4) [19]</p> |

QUESTION/VRAAG 6

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| <p>6.1</p> | | <ul style="list-style-type: none"> ✓ $(-90^\circ ; -3)$ ✓ $(0 ; -1)$ ✓ x – intercepts: -210° & 30° ✓ shape <p style="text-align: right;">(4)</p> |
| <p>6.2</p> | $\cos 2x = 2 \sin x - 1$ $1 - 2 \sin^2 x = 2 \sin x - 1$ $2 \sin^2 x + 2 \sin x - 2 = 0$ $\sin^2 x + \sin x - 1 = 0$ $\sin x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$ $= \frac{-1 \pm \sqrt{1^2 - 4(1)(-1)}}{2(1)}$ $\sin x = \frac{-1 + \sqrt{5}}{2}, \text{ since } \sin x = \frac{-1 - \sqrt{5}}{2} < -1 \text{ has no solution}$ | <ul style="list-style-type: none"> ✓ $\cos 2x = 1 - 2 \sin^2 x$ ✓ standard form ✓ using quadratic formula ✓ substitution into quadratic formula <p style="text-align: right;">(4)</p> |
| <p>6.3</p> | $\sin x = \frac{-1 + \sqrt{5}}{2} = 0,618\dots$ <p>Reference $\angle = 38,17^\circ$</p> <p>$\therefore x = 38,17^\circ + k \cdot 360^\circ$ or $x = 141,83^\circ + k \cdot 360^\circ ; k \in \mathbb{Z}$</p> <p>$\therefore x = 38,17^\circ$ or $-218,17^\circ$</p> <p>$y = 0,24$</p> <p>\therefore Points of intersection/snyppunte: $(38,17^\circ ; 0,24)$ and $(-218,17^\circ ; 0,24)$</p> | <ul style="list-style-type: none"> ✓ $38,17^\circ$ ✓ $141,83^\circ$ ✓ $-218,17^\circ$ ✓ $0,24$ <p style="text-align: right;">(4) [12]</p> |

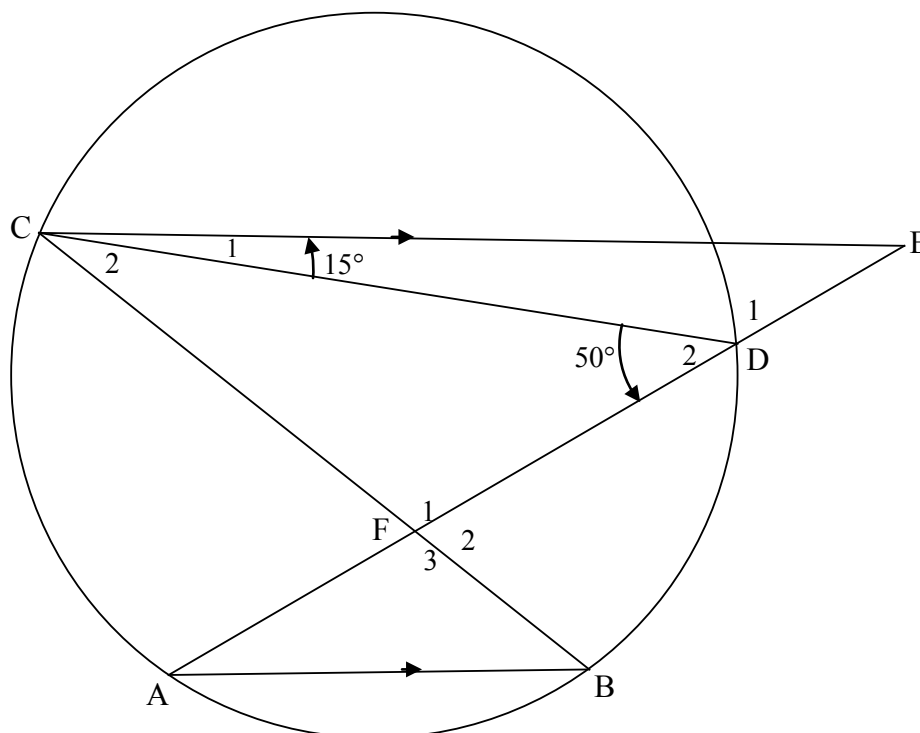
QUESTION/VRAAG 7



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| 7.1 | $\hat{A}BC = 90^\circ$ | ✓ answer (1) |
| 7.2 | <p>In ΔABE:</p> $\frac{AB}{BE} = \tan y$ $AB = k \tan y$ <p>In ΔABC:</p> $\frac{AB}{AC} = \sin x$ $AC = \frac{AB}{\sin x}$ $= \frac{k \tan y}{\sin x}$ | <p>✓ correct ratio</p> <p>✓ value AB</p> <p>✓ correct ratio</p> <p>✓ AC as subject and substitution</p> <p>(4)</p> |

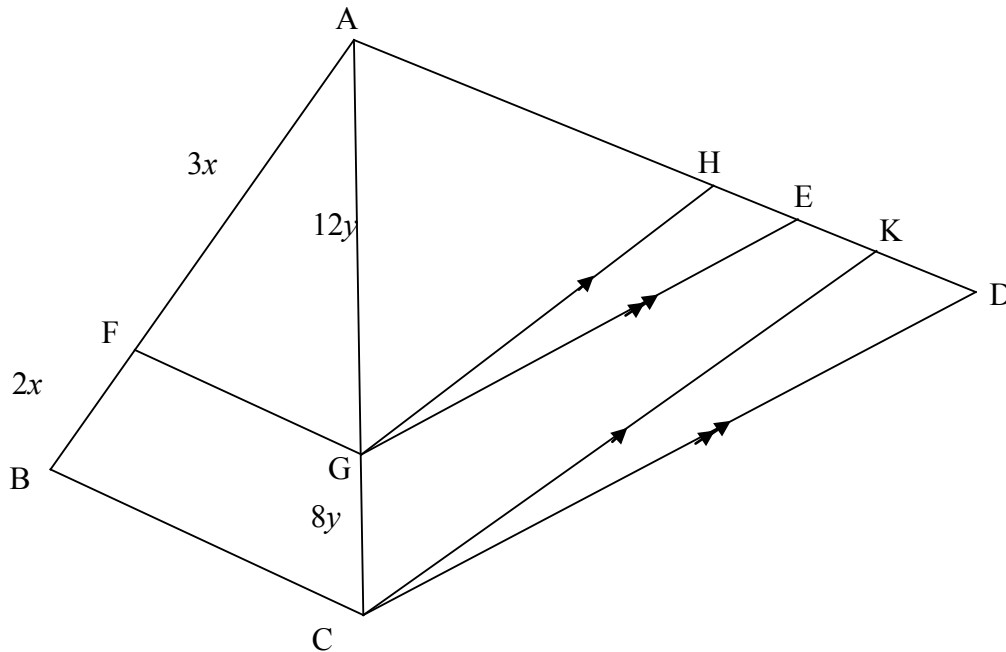
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| <p>7.3</p> | $\hat{A}\hat{D}\hat{C} = \hat{A}\hat{C}\hat{D} = \frac{180^\circ - 2x}{2} = 90^\circ - x$ $\frac{DC}{\sin 2x} = \frac{AC}{\sin(90^\circ - x)}$ $\frac{DC}{2 \sin x \cos x} = \frac{AC}{\cos x}$ $DC = \frac{AC(2 \sin x \cos x)}{\cos x}$ $= \frac{k \tan y}{\sin x} \cdot \frac{2 \sin x \cos x}{\cos x}$ $= 2k \tan y$ <p>OR/OF</p> $DC^2 = AD^2 + AC^2 - 2AD \cdot AC \cos 2x$ $= AC^2 + AC^2 - 2AC^2 \cos 2x$ $= 2AC^2(1 - \cos 2x)$ $= 2AC^2(1 - 1 + \sin^2 x)$ $= 4AC^2 \sin^2 x$ $DC = 2AC \cdot \sin x$ $= 2 \left(\frac{k \cdot \tan y}{\sin x} \right) \cdot \sin x$ $= 2k \cdot \tan y$ <p>OR/OF</p> $DC^2 = AD^2 + AC^2 - 2AD \cdot AC \cos 2x$ $= 2 \left(\frac{k \tan y}{\sin x} \right)^2 - 2 \left(\frac{k \tan y}{\sin x} \right)^2 \cos 2x$ $= \frac{2k^2 \tan^2 y}{\sin^2 x} - \frac{2k^2 \tan^2 y}{\sin^2 x} (1 - 2 \sin^2 x)$ $= \frac{2k^2 \tan^2 y}{\sin^2 x} - \frac{2k^2 \tan^2 y}{\sin^2 x} + 4k^2 \tan^2 y$ $DC = \sqrt{4k^2 \tan^2 y}$ $= 2k \tan y$ | <ul style="list-style-type: none"> ✓ $90^\circ - x$ ✓ subst into sine rule ✓ $2 \sin x \cos x$ ✓ $\cos x$ ✓ substitution (5) ✓ substitution into cos rule ✓ factorisation ✓ $1 - 2 \sin^2 x$ ✓ DC ito AC and $\sin x$ ✓ substitution (5) ✓ correct cos rule ✓ substitution ✓ $1 - 2 \sin^2 x$ ✓ squaring and multiplication ✓ $\sqrt{4k^2 \tan^2 y}$ (5) <p style="text-align: right;">[10]</p> |
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QUESTION/VRAAG 8



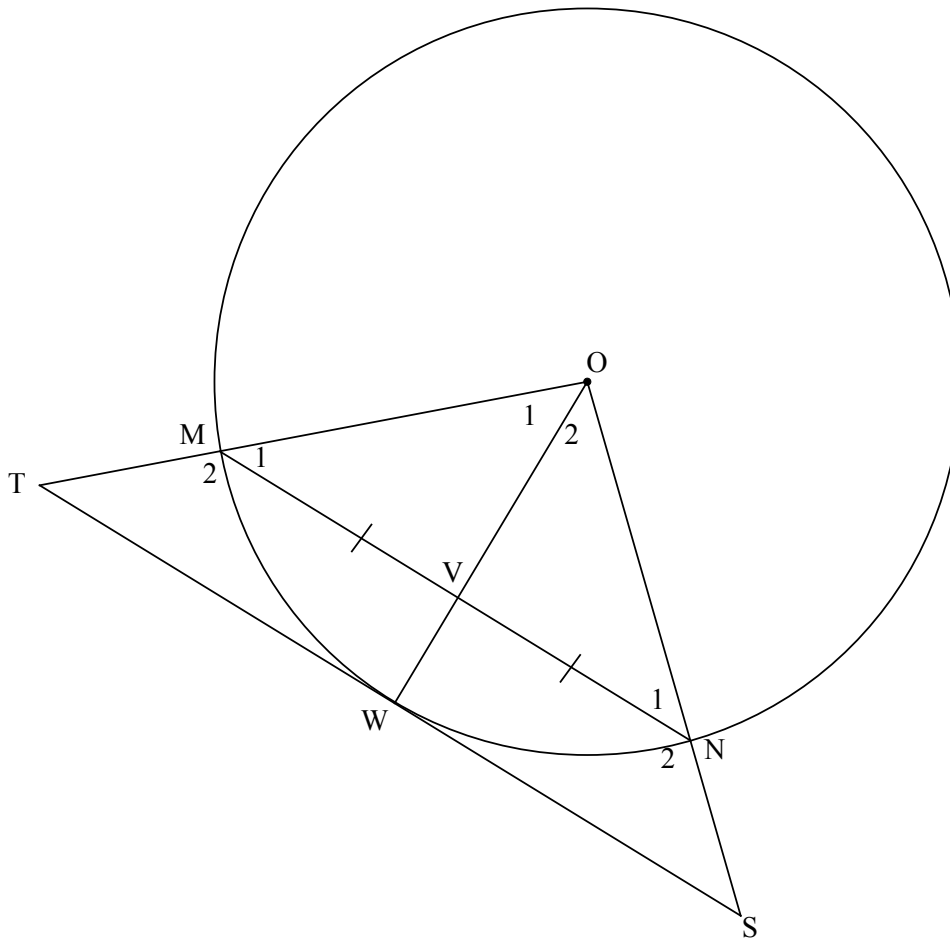
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| <p>8.1.1</p> | <p>$\hat{E} = 50^\circ - 15^\circ = 35^\circ$ [ext \angle of Δ/buite \angle van Δ] $\hat{A} = 35^\circ$ [alt \angles / verwiss \anglee; CE AB]</p> <p>OR/OF $\hat{E} = 180^\circ - (130^\circ + 15^\circ) = 35^\circ$ [str line; \angles of Δ/rt lyn; \anglee van Δ] $\hat{A} = 35^\circ$ [alt \angles / verwiss \anglee; CE AB]</p> <p>OR/OF $\hat{B} = 50^\circ$ [\angles in same segment/\anglee in dieselfde segment] $\hat{C}_2 + 15^\circ = 50^\circ$ [alt \angles / verwiss \anglee; CE AB] $\therefore \hat{C}_2 = 35^\circ$ $\hat{A} = 35^\circ$ [\angles in same segment/\anglee in dieselfde segment]</p> | <p>✓ S ✓ S ✓ R (3)</p> <p>✓ S ✓ S ✓ R (3)</p> <p>✓ S ✓ S ✓ R (3)</p> |
| <p>8.1.2</p> | <p>$\hat{C}_2 = 35^\circ$ [\angles in same segment/\anglee in dieselfde segment]</p> | <p>✓ S ✓ R (2)</p> |
| <p>8.2</p> | <p>$\hat{C}_2 = \hat{E}$ [from 8.1.1 and 8.1.2] \therefore CF is a tangent to the circle [converse tan chord theorem] \therefore CF is 'n raaklyn aan die sirkel [omgekeerde raakl koordst]</p> | <p>✓ S ✓ R (2) [7]</p> |

QUESTION/VRAAG 9



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| <p>9.1.1</p> | $\frac{AF}{BF} = \frac{3x}{2x} = \frac{3}{2} \quad \& \quad \frac{AG}{CG} = \frac{12y}{8y} = \frac{3}{2}$ $\therefore \frac{AF}{BF} = \frac{AG}{CG}$ <p>$\therefore FG \parallel BC$ [conv prop th/omg eweredigh st. OR line divides 2 sides of Δ in prop/lyn verdeel 2 sye v Δ in dies verh]</p> | <p>$\checkmark \frac{AF}{BF} = \frac{AG}{CG}$</p> <p>$\checkmark R$</p> <p style="text-align: right;">(2)</p> |
| <p>9.1.2</p> | $\frac{AG}{GC} = \frac{AH}{HK} \quad \text{[prop theorem/eweredigh st; } \underline{GH \parallel CK} \text{ OR line } \parallel \text{ to 1 side of } \Delta \text{/lyn } \parallel \text{ 1 sy van } \Delta]$ $\frac{AG}{GC} = \frac{AE}{ED} \quad \text{[prop theorem/eweredigh st; } \underline{GE \parallel CD}]$ $\therefore \frac{AH}{HK} = \frac{AE}{ED}$ | <p>$\checkmark S \checkmark R$</p> <p>$\checkmark S$</p> <p style="text-align: right;">(3)</p> |
| <p>9.2</p> | $\frac{AE}{ED} = \frac{3}{2} \quad \text{and} \quad \frac{AH}{HK} = \frac{3}{2}$ $\frac{AE}{12} = \frac{3}{2} \quad \text{and} \quad \frac{15}{HK} = \frac{3}{2}$ <p>$\therefore AE = 18$ and $HK = 10$</p> <p>$\therefore HE = AE - AH$ $= 18 - 15$ $= 3$</p> <p>$\therefore EK = HK - HE$ $= 10 - 3$ $= 7$</p> <p style="text-align: center;">OR/OF</p> <p>$AD = 30$ $KD = AD - AH - HK$ $= 30 - 15 - 10$ $= 5$</p> <p>$EK = ED - KD$ $= 12 - 5$ $= 7$</p> | <p>\checkmark use of ratios</p> <p>$\checkmark AE = 18$</p> <p>$\checkmark HK = 10$</p> <p>$\checkmark HE = 3$ or $KD = 5$</p> <p>$\checkmark EK = 7$</p> <p style="text-align: right;">(5) [10]</p> |

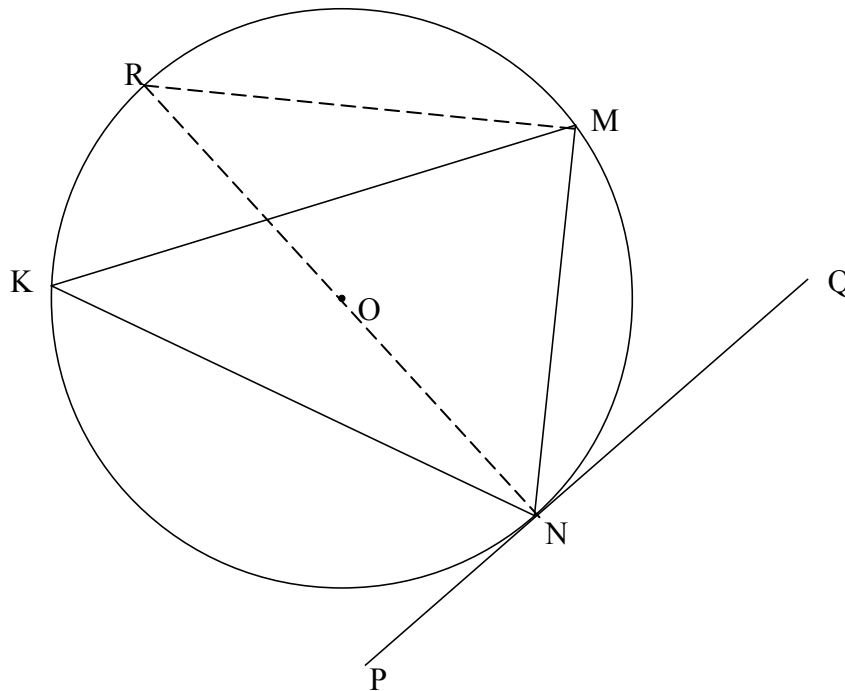
QUESTION/VRAAG 10



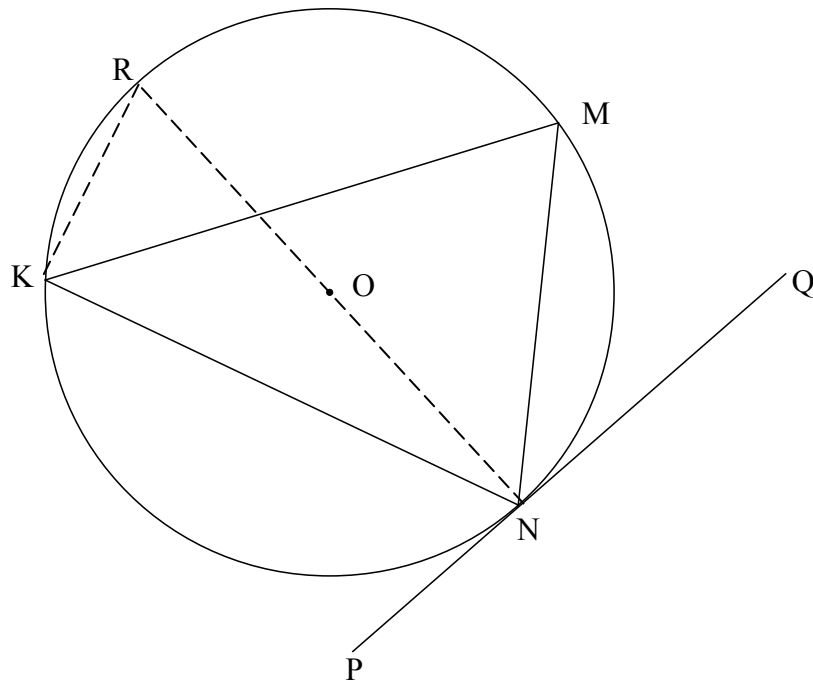
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| 10.1 | Line from centre to midpoint of chord/ <i>lyn vanaf midpt na midpt van koord</i> | ✓ R (1) |
| 10.2.1 | $\widehat{O\hat{W}T} = \widehat{O\hat{W}S} = 90^\circ$ [radius \perp tangent/ <i>raaklyn</i>] $\therefore MN \parallel TS$ [corresp \angle s =/ooreenkomstige \angle e = OR co-int \angle s 180° /ko-binne \angle e 180° OR alternate \angle s/ <i>verwiss \anglee</i>] | ✓ R ✓ R (2) |
| 10.2.2 | $\hat{M}_1 = \hat{N}_1$ [\angle s opp = sides/ \angle e teenoor = <i>sye</i>] $\hat{M}_1 = \hat{T}$ [corresp \angle s/ooreenk \angle e; $MN \parallel TS$] $\therefore \hat{N}_1 = \hat{T}$ \therefore TMNS is a cyclic quadrilateral [conv: ext \angle cyclic quad] TMNS is 'n koordevierhoek [<i>omgek: buite \angle kdvh</i>] OR/OF $\hat{M}_1 = \hat{N}_1$ [\angle s opp = sides/ \angle e teenoor = <i>sye</i>] $\hat{N}_1 = \hat{S}$ [corresp \angle s/ooreenk \angle e; $MN \parallel TS$] $\therefore \hat{S} = \hat{M}_1$ \therefore TMNS is a cyclic quadrilateral [conv: ext \angle cyclic quad] TMNS is 'n koordevierhoek [<i>omgek: buite \angle kdvh</i>] | ✓ S ✓ S ✓ S ✓ R (4) ✓ S ✓ S ✓ S ✓ R (4) |

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| <p>10.2.3</p> | <p>In $\triangle OVN$ and $\triangle OWS$ $\hat{O}_2 = \hat{O}_2$ [common/<i>gemeenskaplik</i>] $O\hat{V}N = O\hat{W}S = 90^\circ$ [from 10.1] $O\hat{N}V = O\hat{S}W$ [sum \angles \triangle/som \anglee \triangle] $\therefore \triangle OVN \parallel \triangle OWS$ [\angle, \angle, \angle] $\therefore \frac{VN}{WS} = \frac{ON}{OS}$ But $VN = \frac{1}{2} MN$ [given] $\therefore \frac{\frac{1}{2} MN}{WS} = \frac{ON}{OS}$ $\therefore OS \cdot MN = 2ON \cdot WS$</p> <p>OR/OF In $\triangle OVM$ and $\triangle OWS$ $O\hat{V}M = O\hat{W}S = 90^\circ$ [from 10.1] $O\hat{M}V = O\hat{S}W$ [sum \angles \triangle/som \anglee \triangle] $\therefore \triangle OVM \parallel \triangle OWS$ [\angle, \angle, \angle] $\therefore \frac{OM}{OS} = \frac{VM}{WS}$ But $VN = \frac{1}{2} MN$ [given] $\therefore \frac{\frac{1}{2} MN}{WS} = \frac{OM}{OS}$ $\therefore OS \cdot MN = 2ON \cdot WS$ [VM = VN]</p> <p>OR/OF If any other 2 \triangles are used, first need to prove that TW = WS by proving $\triangle OWT \equiv \triangle OWS$ In $\triangle OVM$ and $\triangle OWT$ $\hat{O}_1 = \hat{O}_1$ [common/<i>gemeenskaplik</i>] $O\hat{V}M = O\hat{W}T = 90^\circ$ [from 10.1] $O\hat{M}V = O\hat{T}W$ [sum \angles \triangle/som \anglee \triangle] $\therefore \triangle OVM \parallel \triangle OWT$ [\angle, \angle, \angle] $\therefore \frac{VM}{WT} = \frac{OM}{OT}$ But $VN = VM = \frac{1}{2} MN$ [given] and $WT = WS$ and $OT = OS$ [$\triangle OWT \equiv \triangle OWS$] $\therefore \frac{\frac{1}{2} MN}{WS} = \frac{ON}{OS}$ $\therefore OS \cdot MN = 2ON \cdot WS$</p> | <p>✓ S; S; S OR S; S; R</p> <p>✓ $\triangle OVN \parallel \triangle OWS$ ✓ $\frac{VN}{WS} = \frac{ON}{OS}$ ✓ $VN = \frac{1}{2} MN$</p> <p>✓ substitution</p> <p>(5)</p> <p>✓ S; S; S OR S; S; R</p> <p>✓ $\triangle OVM \parallel \triangle OWS$ ✓ $\frac{OM}{OS} = \frac{VM}{WS}$ ✓ $VN = \frac{1}{2} MN$</p> <p>✓ substitution</p> <p>(5)</p> <p>✓ ✓ similarity ✓ ✓ congruency</p> <p>✓ $VN = VM = \frac{1}{2} MN$</p> <p>(5)</p> <p>[12]</p> |
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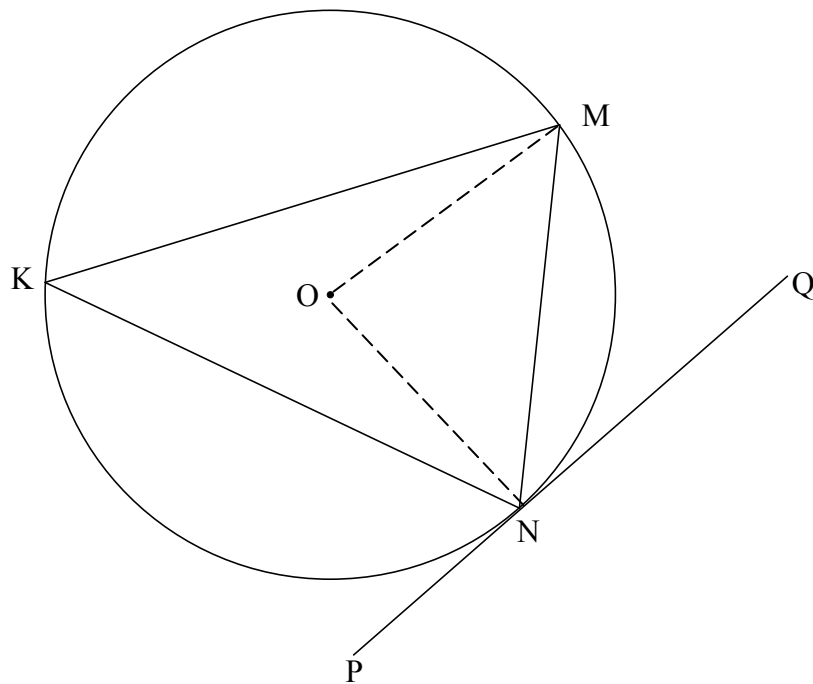
QUESTION/VRAAG 11



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| <p>11.1</p> | <p>Construction: Draw diameter NR and draw RM <i>Konstruksie: Trek middellyn NR en verbind RM</i> $\hat{O}N\hat{M} + \hat{M}\hat{N}Q = 90^\circ$ [radius \perp tangent/raaklyn] $\hat{N}\hat{M}R = 90^\circ$ [\angle in semi circle/semi-sirkel] $\therefore \hat{M}\hat{R}N = 180^\circ - (90^\circ + 90^\circ - \hat{M}\hat{N}Q)$ [sum \angles Δ] $= \hat{M}\hat{N}Q$ but $\hat{M}\hat{R}N = \hat{M}\hat{K}N$ [\angles same segment/\anglee dieselfde segment] $\therefore \hat{M}\hat{N}Q = \hat{K}$ OR/OF</p> | <p>✓ construction ✓ S / R ✓ S / R ✓ S ✓ S / R (5)</p> |
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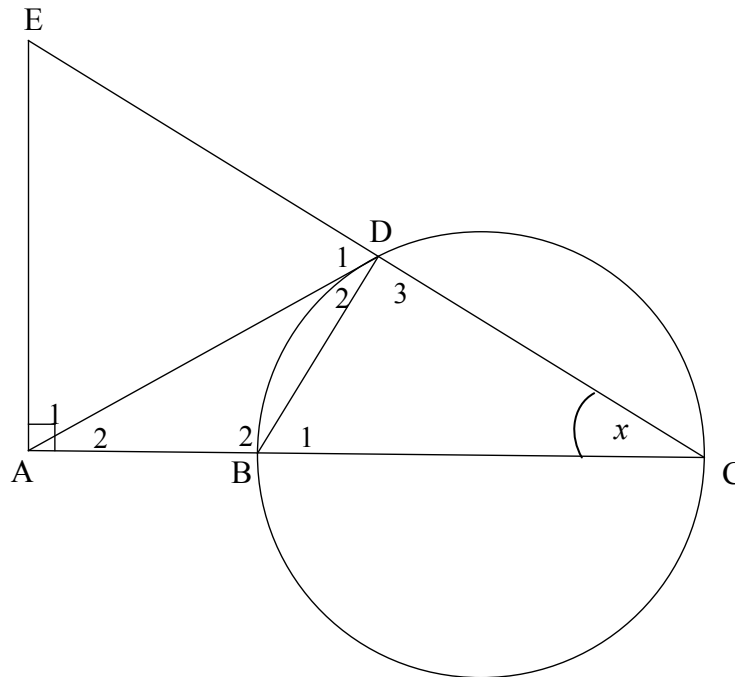


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| <p>11.1</p> | <p>Construction: Draw diameter NR and draw RK <i>Konstruksie: Trek middellyn NR en verbind RK</i> $M\hat{N}Q + R\hat{N}M = 90^\circ$ [radius \perp tangent/raaklyn] $N\hat{K}R = 90^\circ$ [\angle in semicircle/semi-sirkel] $\therefore M\hat{K}N = 90^\circ - R\hat{K}M$ $= 90^\circ - R\hat{N}M$ [\angles same segment/\anglee dieselfde segment] $\therefore M\hat{N}Q = \hat{K}$</p> | <p>✓ construction ✓ S / R ✓ S / R ✓ S ✓ S / R (5)</p> |
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| <p>11.1</p> | <p>Construction: Draw radii ON and OM <i>Konstruksie: Trek radiusse ON en OM</i> $\widehat{M\hat{O}N} = 2\hat{K}$ [\angle at centre = $2\angle$ at circumf/midpts $\angle = 2$ omtreks \angle] $\widehat{O\hat{N}M} + \widehat{O\hat{M}N} = 180^\circ - 2\hat{K}$ [\angles of Δ/ \anglee van Δ] $\widehat{O\hat{N}M} = \widehat{O\hat{M}N} = \frac{180^\circ - 2\hat{K}}{2} = 90^\circ - \hat{K}$ [\angles opp = sides/ \anglee teenoor = sye] $\widehat{O\hat{N}Q} = 90^\circ$ [radius \perp tangent/ radius \perp raaklyn] $\therefore \widehat{M\hat{N}Q} = \hat{K}$</p> | <p>✓ construction ✓ S / R ✓ S ✓ S / R ✓ S / R (5)</p> |
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11.2



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| 11.2.1(a) | Angle in a semi circle/ <i>Hoek in halfsirkel</i> | ✓ R (1) |
| 11.2.1(b) | Exterior \angle of quad = opp interior \angle / <i>Buite \angle van vierh = teenoorst binne \angle</i> OR/OF Opp \angle s of quad supplementary/ <i>Teenoorst \anglee van vierh is supplementêr</i> | ✓ R (1) |
| 11.2.1(c) | tangent chord theorem/ <i>raaklyn koord stelling</i> | ✓ R (1) |
| 11.2.2(a) | In $\triangle AEC$ $\hat{E} = 180^\circ - (90^\circ + x)$ [sum \angle s \triangle] $= 90^\circ - x$ $\hat{D}_1 = 180^\circ - (90^\circ + x)$ [\angle s on a straight line] $= \hat{E} = 90^\circ - x$ $\therefore AD = AE$ [sides opp = \angle s/ <i>syte teenoor = \anglee</i>] | ✓ S ✓ S ✓ R (3) |
| 11.2.2(b) | In $\triangle ADB$ and $\triangle ACD$ $\hat{A}_2 = \hat{A}_2$ [common] $\hat{D}_2 = \hat{C}$ [proven] $\hat{B}_2 = \hat{D}_2 + \hat{D}_3$ [sum \angle \triangle] $\therefore \triangle ADB \parallel \triangle ACD$ OR/OF In $\triangle ADB$ and $\triangle ACD$ $\hat{A}_2 = \hat{A}_2$ [common] $\hat{D}_2 = \hat{C}$ [proven] $\therefore \triangle ADB \parallel \triangle ACD$ [\angle , \angle , \angle] | ✓ S ✓ S ✓ S (3) ✓ S ✓ S ✓ R (3) |

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| <p>11.2.3(a)</p> | $\frac{AD}{AC} = \frac{AB}{AD} \quad [\Delta s]$ $AD^2 = AC \cdot AB$ $= 3r \times r$ $= 3r^2$ | <p>✓ ratio</p> <p>✓ substitution</p> <p>(2)</p> |
| <p>11.2.3(b)</p> | <p>$AD = AE = \sqrt{3}r$ [from 11.2.2(a) & 11.2.3(a)]</p> <p>$AB = r$ and $BC = 2r \therefore AC = 3r$</p> <p><u>In ΔACE:</u></p> $\tan \hat{E} = \frac{AC}{AE}$ $= \frac{3r}{\sqrt{3}r} = \sqrt{3}$ <p>$\therefore \hat{E} = 60^\circ$</p> <p>$\therefore \hat{D}_1 = 60^\circ$ [from 11.2.2(a)]</p> <p>$\therefore \hat{A}_1 = 60^\circ$ [$\angle s$ of $\Delta = 180^\circ$]</p> <p>$\therefore \Delta ADE$ is equilateral/<i>is gelyksydig</i></p> <p>OR/OF</p> $\frac{AD}{AC} = \frac{DB}{CD} \quad [\Delta s]$ $\frac{\sqrt{3}r}{3r} = \frac{DB}{CD}$ $\tan x = \frac{1}{\sqrt{3}}$ <p>\therefore In ΔBDC: $x = 30^\circ$</p> <p>$\therefore \hat{E} = 60^\circ$</p> <p>$\therefore \hat{D}_1 = 60^\circ$ [from 11.2.2(a)]</p> <p>$\therefore \hat{A}_1 = 60^\circ$ [$\angle s$ of $\Delta = 180^\circ$]</p> <p>$\therefore \Delta ADE$ is equilateral/<i>is gelyksydig</i></p> <p>OR/OF</p> $\frac{AD}{AC} = \frac{DB}{CD} \quad [\Delta s]$ $\frac{\sqrt{3}r}{3r} = \frac{DB}{CD} \quad \therefore BD = \frac{CD}{\sqrt{3}}$ $DC^2 = BC^2 - DB^2$ $= 4r^2 - \frac{CD^2}{3}$ $3DC^2 = 12r^2 - CD^2$ $4CD^2 = 12r^2$ $DC = \sqrt{3}r$ | <p>✓ AC ito r</p> <p>✓ trig ratio</p> <p>✓ simplification</p> <p>✓ all 3 $\angle s = 60^\circ$</p> <p>(4)</p> <p>✓ $\frac{\sqrt{3}r}{3r} = \frac{DB}{CD}$</p> <p>✓ $\frac{1}{\sqrt{3}} = \tan x$</p> <p>✓ $x = 30^\circ$</p> <p>✓ all 3 $\angle s = 60^\circ$</p> <p>(4)</p> <p>✓ $BD = \frac{CD}{\sqrt{3}}$</p> <p>✓ $DC = \sqrt{3}r$</p> |

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| | $EC^2 = EA^2 + AC^2$ $= 3r^2 + 9r^2$ $EC = 2\sqrt{3}r$ $\therefore ED = EC - DC$ $= \sqrt{3}r$ $\therefore ED = EA = AD$ $\therefore \triangle ADE \text{ is equilateral/is gelyksydig}$ | $\checkmark EC = 2\sqrt{3}r$ $\checkmark ED = EA = AD$ <p style="text-align: right;">(4) [20]</p> |
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TOTAL/TOTAAL: 150